THERMAL FIELD DYNAMICS AND BIALGEBRAS

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ABSTRACT. In Thermal Field Dynamics, thermal states are obtained from restrictions of vacuum states on a doubled field algebra. It is shown that the suitably doubled Fock representations of the Heisenberg algebra do not need to be introduced by hand but can be canonically handed down from deformations of the extended Heisenberg bialgebra. No artificial redefinitions of fields are necessary to obtain the thermal representations and the case of arbitrary dimension is considered from the beginning. Our results support a possibly fundamental role of bialgebra structures in defining a general framework for Thermal Field Dynamics.

1. INTRODUCTION

Thermal Field Dynamics [1] is based on the idea that thermal states of a quantum system, described by the field algebra $\mathbf{A}$ can be given as restrictions of vacuum states of a doubled algebra of observables $\mathbf{A} \otimes \mathbf{A}$. The doubling of $\mathbf{A}$ is usually given by the so called tilde conjugation rules which can be thought of as a mapping of $\mathbf{A} \cong \mathbf{A} \otimes \mathbf{1}$ into $\mathbf{1} \otimes \mathbf{A}$:

$$(ab)^{\sim} = \tilde{a}\tilde{b}$$
$$(\lambda a + \mu b)^{\sim} = \lambda^* \tilde{a} + \mu^* \tilde{b}$$
$$(\tilde{a})^{\sim} = a$$
$$(a^+)^{\sim} = \tilde{a}^+$$
$$\mid vacuum \rangle^{\sim} = \mid vacuum \rangle$$
$$\text{with } a, b \in \mathbb{C} \text{ and } \lambda, \mu \in \mathbf{A}$$

However the explicit splitting of $\mathbf{A} \otimes \mathbf{A}$ into $\mathbf{A} \otimes \mathbf{1}$ and $\mathbf{1} \otimes \mathbf{A}$ is not necessary. For all intended purposes a doubling from $\mathbf{A}$ to $\mathbf{A} \otimes \mathbf{A}$ without a specification of two copies of $\mathbf{A}$ in $\mathbf{A} \otimes \mathbf{A}$ is sufficient and one can therefore in all the following drop the tilde conjugation rules retaining only the idea of a doubling.

Note, that already at this point the present treatment departs from a different and differently motivated approach to Thermal Field Dynamics based on the modular (Tomita-Takesaki) conjugation as given by I.Ojima [2]. There the modular conjugation realizes an omnipresent tilde conjugation by switching the algebra $\mathbf{A}$ and its commutant $\mathbf{A}'$ in the thermal representation.

Given a vacuum state ω_J on $\mathbf{A}$ one can introduce a doubling $\delta_\chi : \mathbf{A} \to \mathbf{A} \otimes \mathbf{A}$ such that the desired thermal state ω_χ is given by

$$(1) \qquad\qquad \omega_\chi = (\omega_J \otimes \omega_J) \circ \delta_\chi$$

That this is indeed the case is shown in section 2 which reviews also basic facts on the Heisenberg algebra and its exponentiation, the Weyl algebra, mostly omitting proofs. This scheme of producing thermal states has in this setting no deeper justification except that it works.

However, there are two more general points of view:

First, the doubling of the algebra of observables characteristic for Thermal Field Dynamics is just an example of taking tensor products of representations of the field algebra $\mathbf{A}$. A general and systematic way of taking tensor products of representations is given, if $\mathbf{A}$ is equipped with a bialgebra structure [3], so it would be nice to have one on our algebra.

Second, a bialgebra was argued to be possibly the right structure for an axiomatic approach to Thermal Field Dynamics and may thus be assumed from the beginning for a canonical construction of a doubling of the field algebra [4]. In that approach a part of the structure of the theory is deduced from a bialgebra (eventually produced from a symmetry Lie algebra [4,5]) with the rest given by the requirement of a Fock structure. The Fock structure itself can, however, also be cast into a bialgebra form by using the extended Heisenberg algebra (see section 3) thus allowing an axiomatic setting of the theory starting only from a bialgebra.

Both of these points of view ask for a bialgebra. Unfortunately, the Heisenberg algebra $\mathbf{A}$ cannot be turned into one as shown in section 3. However it turns out that by going over to a slightly different algebra, the extended Heisenberg algebra $\mathbf{U}$, one can do away with this problem, and there is a mapping from the extended Heisenberg algebra $\mathbf{U}$ onto the Heisenberg algebra $\mathbf{A}$ that allows to transport interesting structures, particularly the comultiplication Δ responsible for tensor products of representations into the context of physical observables.

This is true even if one q-deforms the extended Heisenberg bialgebra: The deformed extended Heisenberg algebra $\mathbf{U}_\chi$ maps down onto the *undeformed* Heisenberg algebra $\mathbf{A}$ giving thus nothing new for the algebra but providing us with new possible doublings Δ_χ. It is these new doublings Δ_χ coming from deformations of the extended Heisenberg algebra that allow us to express an arbitrary quasifree state in a way similar to Thermal Field Dynamics . This is shown in section 3 together with a discussion of the relevant deformations. The fact that one can produce squeezed states and thermal states by deformations of the extended Weyl algebra has been shown using 1-dimensional examples [6–8]. In particular, a coherent state representation has been exploited and applications to lattice quantum mechanics have been suggested [7,8].

An example showing the relationship between the deformation parameter χ and the inverse temperature of the corresponding thermal state is given in section 4. Section 5 contains conclusions and some general remarks.

2. The Heisenberg algebra and its Weyl form

In order to set the notation it will be shown now that thermal states on a Heisenberg algebra $\mathbf{A}$ can be obtained from a Fock representation (i.e. an irreducible representation obtainable from a vacuum ω_J by the Geĺfand-Naimark-Segal-construction (GNS-construction, see e.g. in O.Bratteli and D.W.Robinson [9]) by a suitable ad hoc doubling. The Heisenberg algebra is generated from a symplectic vector space Γ of arbitrary dimension with the symplectic form $\sigma(\bullet, \bullet)$ by the usual commutation relations:

$$\phi(z_1)\phi(z_2) - \phi(z_2)\phi(z_1) = i\hbar\sigma(z_1, z_2) \qquad\qquad z_1, z_2 \in \Gamma$$

or

$$W(z_1)W(z_2) = e^{\frac{i}{2}\sigma(z_1, z_2)}W(z_1 + z_2) \qquad\qquad z_1, z_2 \in \Gamma$$

Here $\phi(z)$ are the field operators and $W(z)$ their exponentiated Weyl form:

$$W(z) = e^{i\phi(z)}$$

A vacuum state ω_J on the field algebra $\mathbf{A}$ is given by a complex structure J on Γ. On the Weyl generators one has:

$$(2) \qquad\qquad \omega_J(W(z)) = e^{-\frac{1}{4}z\circ J\circ\sigma\circ z}$$

It is also fully determined by its two-point function:

$$\omega_J(\phi(z_1)\phi(z_2)) = \frac{1}{2}z_1 \circ J \circ \sigma \circ z_2$$

The thermal states to be considered are quasifree and thus correspond to free (i.e. quadratic) field Hamiltonians. For each quasifree state there is by the modular theory [10] (Kubo-Martin-Schwinger-theory (KMS-theory, see O.Bratteli and D.W.Robinson [9, 11])) a Hamiltonian with respect to which the state is thermal and therefore one has to show that one can produce any quasifree state of interest by our doubled Fock representations. Any quasifree state corresponding to a positive definite Hamiltonian can be written in the form (compare with O.Bratteli and D.W.Robinson [11],p.50):

$$(3) \qquad\qquad \omega_\chi(W(z)) = e^{-\frac{1}{4}z\circ\coth\frac{\Omega}{2}\circ J\circ\sigma\circ z}$$

where Ω is a positive definite operator arising from the diagonalization of the corresponding Hamiltonian H [12]:

$$(4) \qquad\qquad H = \Omega \circ J \circ \sigma$$

It is known from Thermal Field Dynamics that Ω can be related to a Bogoljubov operator χ on Γ anticommuting with J by the following relation, giving an alternative parametrization of quasifree states:

$$(5) \qquad\qquad \cosh(2\chi) = \coth\frac{\Omega}{2}$$

$$(6) \qquad\qquad \omega_\chi(W(z)) = e^{-\frac{1}{4}z\circ\cosh(2\chi)\circ J\circ\sigma\circ z}$$

with χ satisfying:

$$(7) \qquad\qquad J \circ \chi = -\chi \circ J$$

$$(8) \qquad\qquad \sigma \circ \chi = -\chi \circ \sigma$$

The promised doubling δ_χ is now given by the following action on the Weyl generators:

(9)
$$\delta_\chi(W(z)) = W(\cosh{(\chi)}z) \otimes W(\sinh{(\chi)}z)$$

One can check now by direct calculation that δ_χ is an algebra homomorphism and that it produces from the doubled vacuum state $\omega_J \otimes \omega_J$ the right quasifree state ω_χ:

$$\omega_\chi = (\omega_J \otimes \omega_J) \circ \delta_\chi(W(z)) =$$
$$= (\omega_J \otimes \omega_J)(W(\cosh{\chi}z) \otimes W(\sinh{\chi}z)) =$$
$$= \omega_J(W(\cosh{\chi}z))\omega_J(W(\sinh{\chi}z)) =$$

using (2)

$$= e^{-\frac{1}{4}z\circ\cosh{\chi}\circ J\circ\sigma\circ\cosh{\chi}\circ z}e^{-\frac{1}{4}z\circ\sinh{\chi}\circ J\circ\sigma\circ\sinh{\chi}\circ z} =$$

by (7, 8)

$$= e^{-\frac{1}{4}z\circ(\cosh^2{\chi}+\sinh^2{\chi})\circ J\circ\sigma\circ z} =$$

by the identity $\cosh^2{\chi} + \sinh^2{\chi} = \cosh{2\chi}$

$$= e^{-\frac{1}{4}z\circ\cosh{2\chi}\circ J\circ\sigma\circ z}$$

But this is just the quasifree state (6) that is required.

3. The extended Heisenberg algebra and its deformations

One would like to use a bialgebra structure on a field algebra, in particular the Heisenberg algebra $\mathbf{A}$, and by the GNS-construction a vacuum state ω_J giving a Fock representation, to produce a new representation in which the vacuum doubled by the comultiplication Δ will be a thermal (and thus reducible) state.

There is however a problem with this straightforward idea: There is no bialgebra structure on the Heisenberg algebra $\mathbf{A}$. This can be easily seen from the fact that the Heisenberg commutation relations for the field $\phi(z)$ require a commutator to be proportional to the unit of the algebra.

$$\phi(z_1)\phi(z_2) - \phi(z_2)\phi(z_1) = i\hbar\sigma(z_1, z_2)\mathbf{1}$$

Now, a counit ε of the bialgebra structure has to vanish on commutators and has to be equal to 1 on the unit of the algebra which is not possible unless the proportionality constant in the commutation relations (Planck's constant) is zero.

To improve that, the unit $\mathbf{1}$ of the algebra can be replaced by an abstract central element H. Now it is no more necessary for the counit ε to be equal to $\mathbf{1}$ on this central element, the commutation relations can be considered as a Lie algebra and there exists even a Hopf algebra structure on this extended Heisenberg algebra $\mathbf{U}$ which is actually now a universal enveloping algebra of a Lie algebra [13]. To recover a meaning in the field algebra one can map the extension $\mathbf{U}$ onto the plain Heisenberg algebra $\mathbf{A}$. The map $\Delta^{()} : \mathbf{A} \to \mathbf{A}\otimes\mathbf{A}$ induced from the comultiplication $\Delta : \mathbf{U} \to \mathbf{U} \otimes \mathbf{U}$ is no more preserving the algebra unit but it is a morphism of algebras and thus allows a tensor product of representations.

What is gained by considering the extended Heisenberg algebra $\mathbf{U}$ is the possibility of having an underlying bialgebra structure giving a canonical doubling on the algebra of observables $\mathbf{A}$.

But moreover the extended Heisenberg algebra $\mathbf{U}$ can be deformed without changing the scheme and thus producing new interesting doublings on the Heisenberg algebra. The useful deformations can be found for the one dimensional case in S.Majid [13] and G.Vitiello [14], written in terms of annihilation and creation operators.

In our case the class of possible deformations will be parametrized by a Bogoljubov operator χ on the classical phase space Γ assuming that a vacuum is given by the choice of a complex structure J on Γ. The Bogoljubov operator is characterized by anticommuting with the complex structure J as well as with the symplectic form σ on Γ (7, 8):

$$J \circ \chi = -\chi \circ J$$
$$\sigma \circ \chi = -\chi \circ \sigma$$

Our deformations will break the manifest symplectic group symmetry of the extended Heisenberg algebra $\mathbf{U}$ since χ is not an invariant under these symmetries. They will be written in terms of a set of $\mathbb{R}$-independent eigenvectors $\{z_i, Jz_i\}$.

The deformed commutation relations are:

$$(10) \qquad [\phi(z_i), \pi(z_j)] = -1\delta_{ij}[2H]_{\chi_i}$$

$$(11) \qquad [\phi(z_i), H] = 0$$

$$(12) \qquad [\pi(z_i), H] = 0 \qquad\qquad \text{where } \pi(z_i) := \phi(Jz_i)$$

$$(13) \qquad\qquad\qquad\qquad\qquad \text{and } [x]_{\chi_i} := \frac{\sinh \chi_i x}{\sinh \chi_i}$$

The deformed comultiplication Δ_χ is:

$$(14) \qquad \Delta_\chi \phi(z_i) = \phi(z_i) \otimes e^{\chi_i H} + e^{-\chi_i H} \otimes \phi(z_i)$$

$$(15) \qquad \Delta_\chi \pi(z_i) = \pi(z_i) \otimes e^{\chi_i H} + e^{-\chi_i H} \otimes \pi(z_i)$$

$$(16) \qquad \Delta_\chi H = H \otimes \mathbf{1} + \mathbf{1} \otimes H$$

It can be checked by direct calculation that the comultiplication Δ preserves the commutation relations and that it is coassociative:

$$(17) \qquad [\Delta_\chi \phi(z_i), \Delta_\chi \pi(z_i)] = -1\delta_{ij}[2\Delta_\chi H]_{\chi_i}$$

$$(18) \qquad (\Delta_\chi \otimes \mathbf{1}) \circ \Delta_\chi = (\mathbf{1} \otimes \Delta_\chi) \circ \Delta_\chi$$

In the Weyl form the deformed commutation relations and the comultiplication can be written as:

$$(19) \qquad U(z_i)V(z_j) = e^{-i[2H]_{\chi_i}} V(z_j)U(z_i)$$

$$(20) \qquad \Delta_\chi U(z_i) = U(e^\chi z_i) \otimes U(e^{-\chi} z_i)$$

$$(21) \qquad \Delta_\chi V(z_i) = V(e^\chi z_i) \otimes V(e^{-\chi} z_i)$$

with:

$$(22) \qquad U(z_i) := e^{i\phi(z_i)} = W(z_i)$$

$$(23) \qquad V(z_i) := e^{i\pi(z_i)} = W(Jz_i)$$

We turn now to the canonical mappings p, p_n of the deformed extended Heisenberg algebra $\mathbf{U}_\chi$ and its coproducts $\Delta_\chi^{n-1}\mathbf{U}_\chi$ onto the Heisenberg algebra $\mathbf{A}$ and its tensor products $\mathbf{A}^{\otimes n}$. It will be required that p, p_n are algebra homomorphisms and that H as well as $\Delta_\chi^{n-1}H$ are mapped by p, p_n into the units $\mathbf{1}$, $\mathbf{1}^{\otimes n}$. In the following the generators $\phi(z_i)$, $\pi(z_i)$ will be identified with their images $p(\phi(z_i))$, $p(\pi(z_i))$.

The map p is fully specified and it is thus tempting to set $p_n = p^{\otimes n}$, but then $\Delta_\chi^{n-1}H$ would be mapped into $n \cdot \mathbf{1}$ instead of $\mathbf{1}$. To fix the normalization one has to set:

$$(24) \qquad p_n(\Delta_\chi^{n-1}\phi(z_i)) = \frac{1}{\sqrt{n}}p^{\otimes n}(\Delta_\chi^{n-1}\phi(z_i))$$

$$(25) \qquad p_n(\Delta_\chi^{n-1}\pi(z_i)) = \frac{1}{\sqrt{n}}p^{\otimes n}(\Delta_\chi^{n-1}\pi(z_i))$$

Now p_n is also fully specified. The important thing now is that the map $\Delta_\chi^{n-1} : \mathbf{U}_\chi \to \mathbf{U}_\chi^{\otimes n}$ factors through the maps p, p_n as can be checked on the generators. The result is a map

$$(26) \qquad \Delta_\chi^{(n-1)} : \mathbf{A} \to \mathbf{A}^{\otimes n}$$

which fills in the commutative diagram

$$(27) \qquad
\begin{array}{ccc}
\mathbf{U}_\chi & \xrightarrow{\ p\ } & \mathbf{A} \\
{\scriptstyle \Delta_\chi^{n-1}}\downarrow & & \downarrow{\scriptstyle \Delta_\chi^{(n-1)}} \\
\mathbf{U}_\chi^{\otimes n} & \xrightarrow[\ p_n\ ]{} & \mathbf{A}^{\otimes n}
\end{array}$$

The map $\Delta_\chi^{(n-1)}$ is an algebraic homomorphism and allows thus to take tensor products of representations. Note however, that due to the necessary normalization $\Delta_\chi^{(n-1)}$ is not a comultiplication.

In the case $n = 2$, $\Delta_\chi^{(1)}$ is our canonical doubling. If we use now this canonical doubling for doubling a vacuum state ω_J and the corresponding Fock representation, one obtains the state ω_χ:

$$\omega_\chi(U(z_i)) \equiv \omega_\chi(W(z_i)) =$$
$$= (\omega_J \otimes \omega_J) \circ \Delta_\chi^{(1)}(U(z_i)) =$$
$$= (\omega_J \otimes \omega_J)(U(e^\chi \frac{z_i}{\sqrt{2}}) \otimes U(e^\chi \frac{z_i}{\sqrt{2}})) =$$
$$= e^{-\frac{1}{4}(\frac{1}{2}z_i \circ e^\chi \circ J \circ \sigma \circ e^\chi \circ z_i)} e^{-\frac{1}{4}(\frac{1}{2}z_i \circ e^{-\chi} \circ J \circ \sigma \circ e^{-\chi} \circ z_i)} =$$
$$= e^{-\frac{1}{4}(z_i \circ \frac{(e^{2\chi}+e^{-2\chi})}{2} \circ J \circ \sigma \circ z_i)} =$$
$$= e^{-\frac{1}{4}(z_i \circ \cosh 2\chi \circ J \circ \sigma \circ z_i)}$$

and similarly:

$$\omega_\chi(V(z_i)) \equiv \omega_\chi(W(Jz_i)) =$$
$$= e^{-\frac{1}{4}(Jz_i \circ \cosh 2\chi \circ J \circ \sigma \circ Jz_i)}$$

By extension from the generators one gets:

$$(28) \qquad \omega_\chi(W(z_i)) = e^{-\frac{1}{4}(z_i \circ \cosh 2\chi \circ J \circ \sigma \circ z_i)}$$

But this is just the quasifree state (6).

4. An Example: The Harmonic oscillator

In the special case of a 1-dimensional harmonic oscillator some particular simplifications occur. In its 2-dimensional phase space $\Gamma \cong \mathbb{R}^2$ there exists a basis in which the symplectic form σ, the complex structure J and the given Bogoljubov operator χ take the form:

$$(29) \qquad \sigma_{ab} = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$$

$$(30) \qquad J^a{}_b = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$$

$$(31) \qquad \chi^a{}_b = \begin{pmatrix} \chi & 0 \\ 0 & -\chi \end{pmatrix}$$

This basis is unique and can be given also by geometrical considerations unless $\chi = 0$. Using J as the imaginary unit one can now identify the phase space Γ with the complex numbers:

$$(32) \qquad \Gamma \cong \mathbb{C}$$

The vacuum state ω_J and the state ω_χ obtained in (28) are then given by:

$$(33) \qquad \omega_J(W(z)) = e^{-\frac{1}{4}\|z\|^2}$$

$$(34) \qquad \omega_\chi(W(z)) = e^{-\frac{1}{4}\cosh 2\chi \|z\|^2}$$

The Hamiltonians compatible with the complex structure J (i.e. those which have a diagonalization (4) giving the fixed J) are determined by the matrix

$$(35) \qquad H_{ab} = E\beta \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

The corresponding thermal states are

$$(36) \qquad \omega_\beta(W(z)) = e^{-\frac{1}{4}\coth\frac{\beta E}{2}\|z\|^2}$$

Fixing E as the energy of the harmonic oscillator and comparing (34) and (36) the states ω_χ are identified with the thermal states, ω_β, of the Hamiltonian at inverse temperature β, obtaining the relation

$$(37) \qquad \coth\frac{\beta E}{2} = \cosh 2\chi$$

between the inverse temperature β and the deformation parameter χ. So, in the end, the deformation parameter χ has a nice interpretation as a function of the inverse temperature.

5. Conclusion

It is shown that there is a class of deformations of the extended Heisenberg bialgebra $\mathbf{U}_\chi$ that provide canonical doublings by mapping down their comultiplications on the Heisenberg algebra $\mathbf{A}$. These doublings give directly, without any redefinitions, all representations arising from quasifree states by the GNS-construction. In particular the doublings give all thermal representations for free Hamiltonians. Our construction works clearly for any finite dimensional system and on the level of calculus also for infinite dimensional systems. Functional analytic discussions for the infinite dimensional case are omitted. Note, however, that at no point unitary equivalence of representations is used and that all Bogoljubov transformations are given by symplectomorphisms on the classical phase space. Thus no problem is expected in extending our considerations to the infinite dimensional case.

It would be useful to know if there are other deformations other, than the ones used here, of the extended Heisenberg algebra $\mathbf{U}$. If not, then the construction becomes entirely canonical, since the class of deformations appears to be the only choice one could make in the construction. If there are other deformations then it would be interesting to see the interpretation of the induced doublings on the Heisenberg algebra $\mathbf{A}$ arising from them.

In any case the present results show that the bialgebra structure is a logical way to approach Thermal Field Theory by providing both the correct results and a mathematically satisfactory general structur.

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